

Kinetic Energy

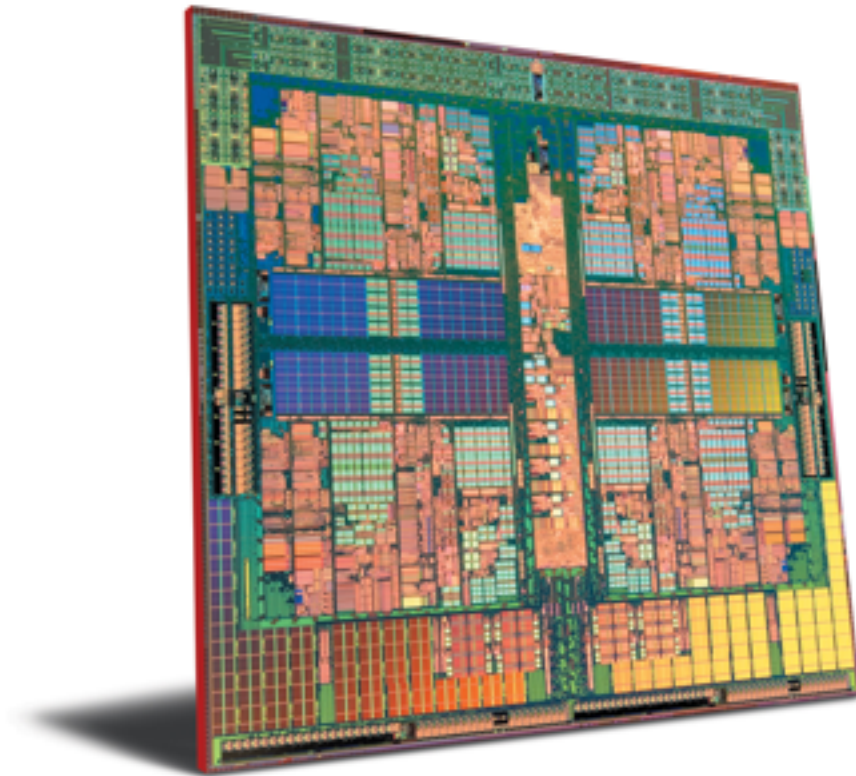
A blurred photograph of a train station platform. A train is visible in the background, and several people are walking in the foreground. The image is intentionally out of focus to convey a sense of motion and energy.

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Humans
move things



moving rocks



moving
electrons

To get things moving, we need to exert a force.

Newton's second law:

$$\mathbf{Force = mass * acceleration (F = ma)}$$

so also

$$\mathbf{acceleration = force / mass}$$

SI Units:

1 Newton force = 1 kg mass * 1 m/s/s acceleration

Other units:

- “Lbs” or “pounds mass” is mass in English measure (also, “slugs”!)
- “Pounds force” is force in English measure

From google (you can type in equations and google handles the units):



$$(1 \text{ kg}) * 1 ((\text{meter} / \text{second}) / \text{second}) = 1 \text{ newton}$$

This leads to definitions for energy and work in physics:

Work is done when a force is applied through a distance.

Energy is the **capacity for doing work**. So:

$$\text{Energy} = \text{force} * \text{distance}$$

SI Units:

1 **Joule** energy = 1 Newton force * 1 Meter distance

(Since a newton is a unit of force, and $F=ma$, we can reduce this to:

$$1 \text{ joule} = \text{kg} * 1 \text{ m} / \text{s} / \text{s} * 1 \text{ m})$$



$$(1 \text{ newton}) * 1 \text{ meter} = 1 \text{ joule}$$



$$((1 \text{ kg}) * (1 \text{ (m}^2\text{)})) / (1 \text{ (s}^2\text{)}) = 1 \text{ joule}$$

Power is the rate of work.

$$\text{Power} = \text{Energy} / \text{Time}$$

SI Units:

1 **Watt** power = 1 Joule energy / 1 second time

so also

1 Joule = 1 Watt * 1 second



$$(1 \text{ joule}) / (1 \text{ second}) = 1 \text{ watt}$$

We can perform work against the force of gravity to store energy in the position of objects in a gravitational field.

$$\text{Gravitational Potential Energy} = mgh$$

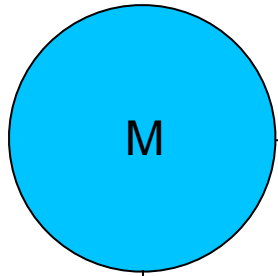
m = mass

g = gravitational acceleration = 9.8 m/s/s

h = height



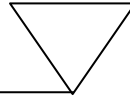
$$(1 \text{ kg}) * (9.8 ((\text{m} / \text{s}) / \text{s})) * (1 \text{ meter}) = 9.8 \text{ joules}$$



M



g



h

$$PE = mgh$$

Kinetic energy is the energy of objects in motion:

$$\mathbf{Kinetic\ Energy = \frac{1}{2} mv^2}$$

m = mass in kg

v = velocity in meters/second



$$(1 / 2) * (1 \text{ kg}) * ((1 \text{ (m / s)})^2) = 0.5 \text{ joules}$$

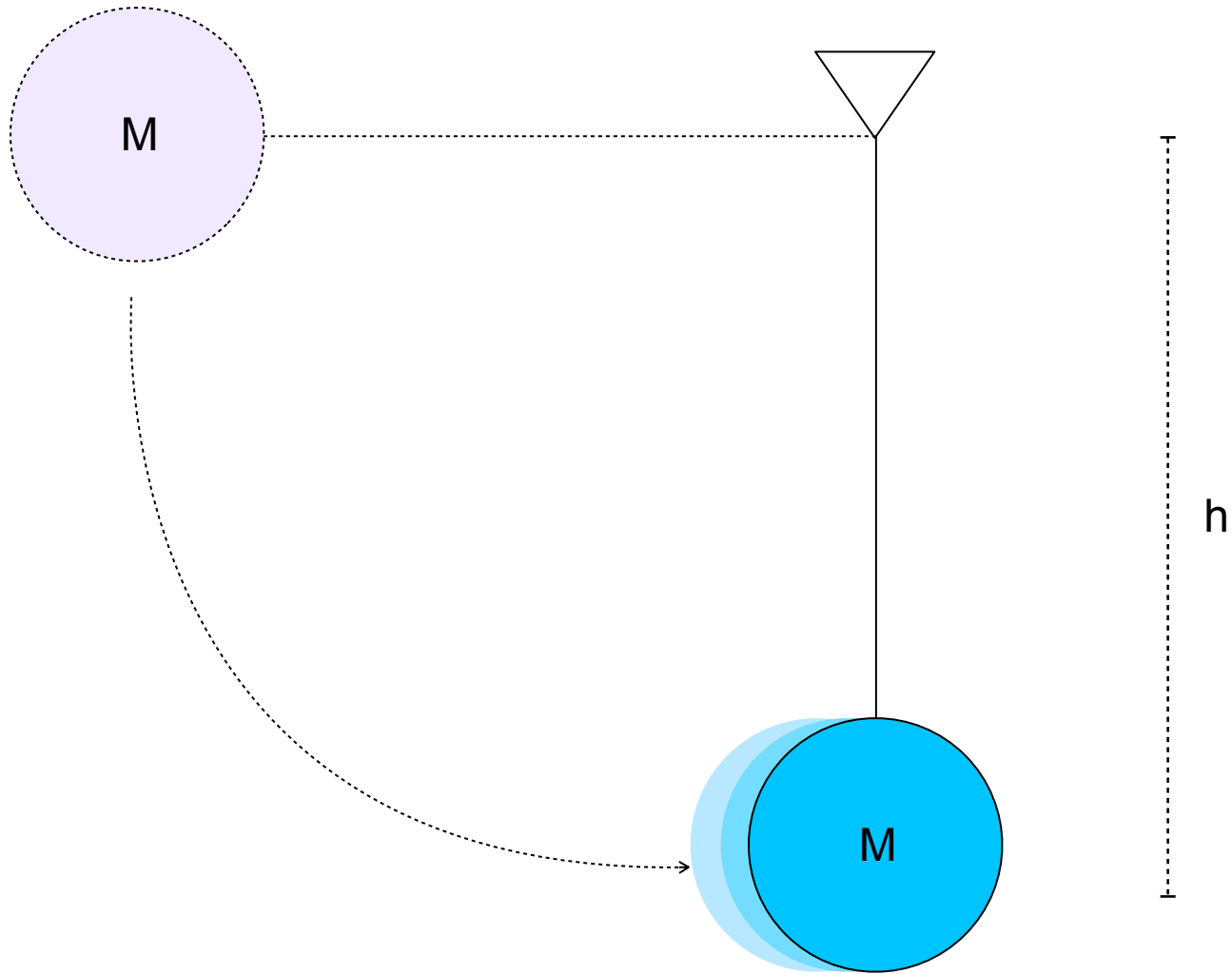
Rotational Work

Same as linear work, but the force is traveling in a circle.

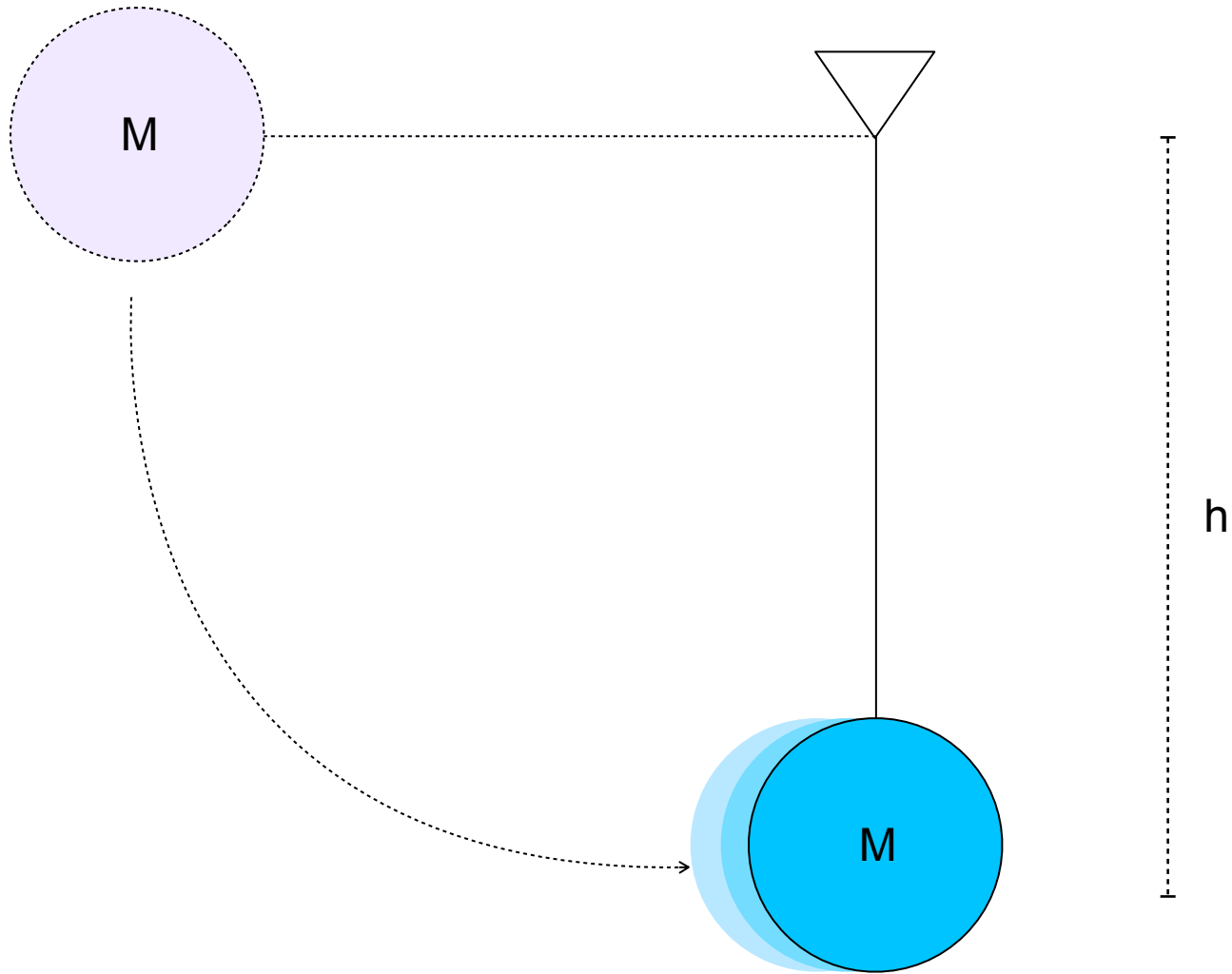
So 1 Newton force applied to a 1 meter lever pushed through 360 degrees = 6.28 Joules (The force moves through the circumference of the circle = 2 pi meters)



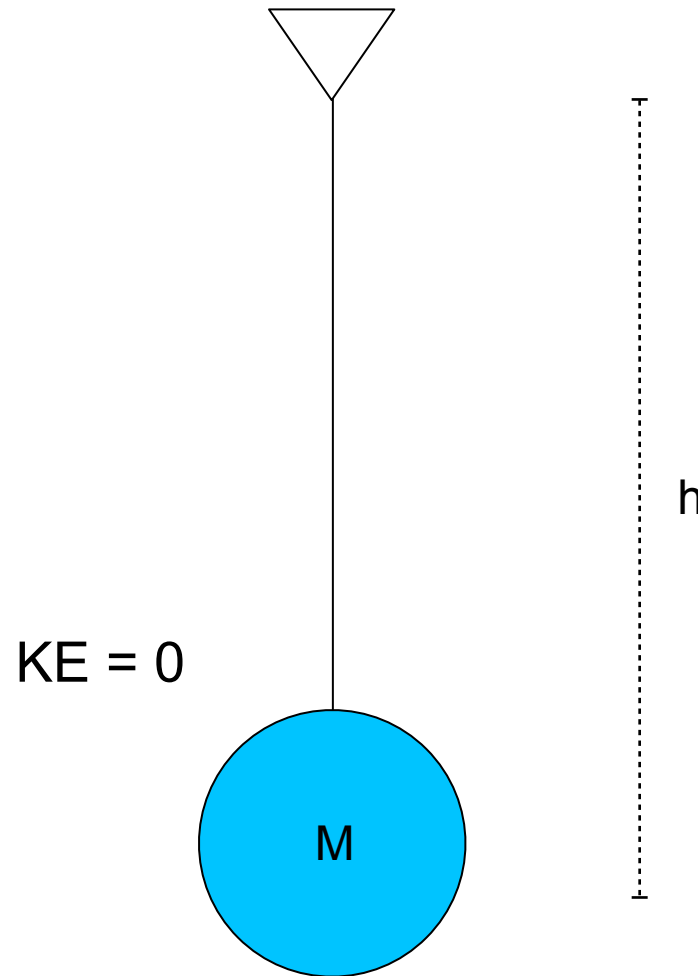
$$(1 \text{ newton}) * 1 \text{ meter} * (360 \text{ degrees}) = 6.28318531 \text{ joules}$$



$$KE = \frac{1}{2} mv^2$$



On first swing, from 1st Law we know:
 $KE \approx PE$ (energy is conserved)



At end, we note 1st and 2nd laws. All of the original PE is *somewhere* (heat, noise, etc.), but is more diffuse and less useful to us.

Most important take away:

We can't get work out of a system that isn't in the system in the first place.

aka 1st law

aka "You can't win"

Not all of the energy in a system will be available to do the work we want.

aka 2nd law

aka "You can't break even"

Next most important take away:

$$\text{Power (watts)} = \text{Energy (joules)} / \text{time (seconds)}$$

Energy is a quantity. Power is a rate.

Technical take away:

We can make estimates of energy in systems (potential energy, kinetic energy) if we know mass, force, velocity, etc.

We can use these estimates to form maximum outside bounds as to the useful work we could get from a system.